

AP CHEMISTRY

TOPIC 12: SOLUTIONS, REVIEW, PART I

Day 136:

1. Lead(II) bromide dissociates in water and has a $K_{sp} = 4.6 \times 10^{-6}$ at 25°C

a) Write the chemical dissociation equation for the above dissociation.



b) Write the equilibrium expression

$$K_{sp} = [\text{Pb}^{+2}] [\text{Br}^{-1}]^2$$

c) Calculate the concentration, in mol L^{-1} of the bromide ions in a saturated solution of lead(II) bromide at 25°C .

	PbBr_2	\leftrightarrow	Pb^{+2}	+	2Br^{-1}
I	-		0		0
C	-		+ x		+ $2x$
E	-		x		$2x$

$$4.6 \times 10^{-6} = [\text{Pb}^{+2}] [\text{Br}^{-1}]^2$$

$$4.6 \times 10^{-6} = [x] [2x]^2 = 4x^3$$

$$x = 1.05 \times 10^{-2} \text{ M} = [\text{Pb}^{+2}]$$

$$[\text{Br}^{-1}] = 2x = (2)(1.05 \times 10^{-2} \text{ M}) = 2.10 \times 10^{-2} \text{ M}$$

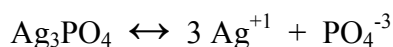
d) Calculate the maximum mass, in grams, of lead(II) bromide that can dissolve in 4297 mL of water at 25°C .

$$\frac{4297 \text{ mL}}{1000 \text{ mL}} \times \frac{1 \text{ L}}{1 \text{ L}} \times \frac{1.05 \times 10^{-2} \text{ mol Pb}^{+2}}{1 \text{ L}} \times \frac{1 \text{ mol PbBr}_2}{1 \text{ mol Pb}^{+2}} \times \frac{367 \text{ g}}{1 \text{ mol PbBr}_2} = 16.6 \text{ g}$$

2. In a saturated solution of silver phosphate at 25°C , the concentration of $\text{PO}_4^{-3} (aq)$ is $1.6069 \times 10^{-5} \text{ M}$. The equilibrium constant expression for the dissolving of silver phosphate in water is shown below:

$$K_{sp} = [\text{Ag}^{+1}]^3 [\text{PO}_4^{-3}]$$

a) Write the balanced equation for the dissolving of silver phosphate in water.



b) Calculate the value of K_{sp} for silver phosphate at 25°C .

	Ag_3PO_4	\leftrightarrow	3Ag^{+1}	+	PO_4^{-3}
I	-		0		0
C	-		+ $3x$		+ x
E	-		$3x$		x

$$[\text{PO}_4^{-3}] = 1.6069 \times 10^{-5} \text{ M} = x$$

$$[\text{Ag}^{+1}] = \frac{1.6069 \times 10^{-5} \text{ mol}}{1 \text{ L}} \times \frac{3 \text{ mol Ag}^{+1}}{1 \text{ mol PO}_4^{-3}} = 4.821 \times 10^{-5} \text{ M} = 3x$$

$$K_{sp} = (4.821 \times 10^{-5})^3 (1.6069 \times 10^{-5}) = 1.8 \times 10^{-18}$$

3. A solution is prepared by dissolving 144 grams barium hydroxide ($K_{sp} = 5.0 \times 10^{-3}$) in 3500 mL of water. Calculate the freezing point of this solution. (Hint: you have a K_{sp} value which indicates that the salt is NOT strong and that this salt does not dissociate to 100% - calculate the number of moles that do dissociate.)

$$K_{sp} = [\text{Ba}^{+2}] [\text{OH}^{-1}]^2$$

	Ba(OH) ₂	⇌	Ba ⁺²	+	2 OH ⁻¹
I	-		0		0
C	-		+ x		+ 2x
E	-		x		2x

$$5.0 \times 10^{-3} = [\text{Ba}^{+2}] [\text{OH}^{-1}]^2$$

$$5.0 \times 10^{-3} = [x] [2x]^2 = 4x^3$$

$$\frac{5.00 \times 10^{-3}}{4} = 0.00125 \quad ; \quad x = \sqrt[3]{0.00125} = 0.10772 = [\text{Ba}^{+2}]$$

$$\frac{3500 \text{ mL}_{\text{H}_2\text{O}}}{1 \text{ mL}_{\text{H}_2\text{O}}} \times \frac{1 \text{ g}_{\text{H}_2\text{O}}}{1000 \text{ g}_{\text{H}_2\text{O}}} \times \frac{0.10772 \text{ mol Ba}^{+2}}{1 \text{ kg}_{\text{H}_2\text{O}}} \times \frac{1 \text{ mol Ba(OH)}_2}{1 \text{ mol Ba}^{+2}} = 0.377 \text{ mol Ba(OH)}_2$$

$$\Delta T_f = i k_f \text{ molality} \quad ; \quad \Delta T_f = (3) \left(\frac{1.86 \text{ kg}}{\text{mol}} \right) \left(\frac{0.3770 \text{ mol}}{3.50 \text{ kg}} \right) = 0.601^\circ \text{C}$$

$$\text{F.P. for water} = 0^\circ \text{C} - 0.601^\circ \text{C} = -0.601^\circ \text{C}$$

You do NOTHING with the 144 grams... This is to “distract you” – focus on WHAT the question is asking... This IS a past AP Exam question...

4. A solution containing 365.3 grams of an electrolyte (that dissociates into four particles) dissolved in 1200 grams of water boils at 107.44°C . Calculate the approximate molecular weight of the solute.

$$\Delta T_b = 107.44^{\circ}\text{C} - 100^{\circ}\text{C} = 7.44^{\circ}\text{C}$$

$$1200 \text{ grams} = 1.20 \text{ kilograms}$$

$$\Delta T_b = i k_b \text{ molality}$$

$$7.44^{\circ}\text{C} = \frac{(4) 0.51^{\circ}\text{C} \cdot \text{kg}}{(\text{mol})} \left(\frac{? \text{ mol}}{1.2 \text{ kg}} \right)$$

$$? \text{ mol} = \frac{(7.44^{\circ}\text{C})(1.2 \text{ kg}_{\text{H}_2\text{O}})(\text{mol})}{(4) (0.51^{\circ}\text{C} \cdot \text{kg})} = 4.376 \text{ mol}$$

$$\text{molecular weight} = \frac{365.3 \text{ g solute}}{4.376 \text{ mol solute}} = 83.5 \frac{\text{g}}{\text{mol}}$$

5. What mass of aluminum perchlorate must be dissolved in 3.53 kg of water to give a solution with a freezing point of -13.33°C ?

$$\Delta T_f = (4) (1.86^{\circ}\text{C} \cdot \text{kg} \cdot \text{mol}^{-1}) (\text{molality}) = 13.33^{\circ}\text{C}$$

$$13.33^{\circ}\text{C} = \frac{(4) 1.86^{\circ}\text{C} \cdot \text{kg}}{(\text{mol})} \left(\frac{? \text{ mol}}{3.53 \text{ kg}} \right)$$

$$\text{moles} = \frac{(13.33^{\circ}\text{C})(3.53 \text{ kg}_{\text{H}_2\text{O}})(\text{mol})}{(4) (1.86^{\circ}\text{C} \cdot \text{kg})} = 6.32458 \text{ mol}$$

$$\frac{6.32458 \text{ mol}}{1} \times \frac{325.33 \text{ g}}{\text{mol}} = 2.06 \times 10^3 \text{ g Al}(\text{ClO}_4)_3$$