TOPIC 3: GASES, TEST REVIEW

- Boyle, Charles, and Avogadro: Gas Laws
- Ideal Gas Law
- Gas Stoichiometry
- Gas Density

- Gas Molar Mass
- Dalton's Law of Partial Pressures
- Gas collection over Water
- Kinetic Molecular Theory of Gases

Day 43:

- Effusion and Diffusion
- Root mean square velocity
- Real Gases (van der Waals)
- 1) A compressed gas cylinder contains 45.22 liters of neon gas at a pressure of 4732.0 torr at a temperature of 36.4 °C. What is the new volume if the pressure is reduced to 3000.0 torr and at a new temperature of 13.56 °C.

Answers:

$$P_1V_1 = nRT_1$$

$$P_2V_2 = nRT_2$$

$$P_2V_2 = nRT_2$$
 $36.4 + 273 = 309.4 \text{ K}, 13.56 + 273 = 286.56 \text{ K}$

$$V_2 = \frac{P_1 V_1 T_2}{P_2 T_1} = \frac{(4732.0 \ torr)(45.22 \ L)(286.56 \ K)}{(3000.0 \ torr)(309.4 \ K)} = 66.1 \ L$$

2) A 8.00 liter sample of butane gas, C₄H₁₀, reacts with a 24.0 liter sample of oxygen gas at 40.2 °C and at a pressure of 1.460 atm. Calculate the volume of the carbon dioxide gas formed at a new temperature of 103 °C and at a pressure of 3.10 atm.

Answers:

$$2 C_4H_{10} + 13 O_2 \rightarrow 10 H_2O + 8 CO_2$$

$$n_{C_4H_{10}} = \frac{PV}{RT} = \frac{(1.460 \ atm) (mol \cdot K)(8.0 \ L)}{(0.0821 \ atm \cdot L)(313.2 \ K)} = 0.45423 \ mol \ C_4H_{10}$$

$$n_{oxygen} = \frac{PV}{RT} = \frac{(1.460 \ atm) (mol \cdot K)(24.0 \ L)}{(0.0821 \ atm \cdot L)(313.2 \ K)} = 1.3627 \ mol \ O_2$$

$$\frac{1.3627 \ mol \ O_{2}}{13 \ mol \ O_{2}} \times \frac{2 \ mol \ C_{4}H_{10}}{13 \ mol \ O_{2}} = 0.20965 \ mol \ C_{4}H_{10} \ ; \ \textit{O}_{2} \ \textit{is the limiting reactant}$$

$$\frac{1.3627 \ mol \ O_2}{13 \ mol \ O_2} \times \frac{8mol \ CO_2}{13 \ mol \ O_2} = 0.8386 \ mol \ CO_2$$

$$PV=nRT$$
; $V=\frac{nRT}{P}$

$$V = \frac{(0.8386 \ mol)(0.0821 \ atm \cdot L)(376 \ K)}{(3.10 \ atm)(mol \cdot K)} = 8.35 \ L \ CO_2$$

3) Calculate the density of a sample of gas at STP that has a molar mass of 164.3 g mol⁻¹.

Answers:

$$\frac{m}{V} = \frac{PM}{RT}$$

$$\frac{m}{V} = \frac{PM}{RT} = \frac{(1.00 \ atm) (mol \cdot K) (164.3 \ g)}{(0.0821 \ atm \cdot L) (273 \ K) (mol)} = 7.330 \ g \ L^{-1}$$

4) The density of a gas was measured at 3.33 atm and 16.45 0 C and found to be 4.97 g/L. Calculate the molar mass of this gas.

Answers:

$$PV=nRT$$

$$PV = \frac{m}{M}RT$$
 therefore, $M = \frac{m}{V} \times \frac{RT}{P}$

$$M = \frac{4.97 \ g}{L} \times \frac{(0.0821 \ atm \cdot L)(289.45 \ K)}{(3.33 \ atm)(mol \cdot K)} = 35.5 \ g \ mol^{-1}$$

5) Hydrogen gas is produced from a chemical reaction and collected over water at 25 °C and 1.07 atm total pressure. What total volume of gas must be collected to obtain 3.80 grams of hydrogen gas? (At 25 °C the vapor pressure of water is 23.8 torr.)

Answers:

$$P_{H_2} + P_{H_2O} = 1.07 _atm = 813.2 _torr = P_{H_2} + 23.8 _torr, = P_{H_2} = 789.4 _torr$$

$$n_{H_2} = \frac{3.80 \ g \ H_2}{2.0158 \ g} \times \frac{1 \ mol \ H_2}{2.0158 \ g} = 1.8851 \ mol \ H_2$$

$$V = \frac{nRT}{P} = \frac{(1.8851 \ mol)(0.0821 \ atm \cdot L)(298 \ K)}{(1.0387 \ atm)(mol \cdot K)} = 44 \ L \ H_2$$

6) How many times faster would nitrogen gas, N₂, diffuse than sulfur tri-oxide gas, SO₃?

Answers:

$$N_2 = 28.014 \ g \ mol^{-1}$$

 $SO_3 = (32.06 \ g \ mol^{-1}) + (3)(16.00 \ g \ mol^{-1}) = 80.06 \ g \ mol^{-1})$

$$\frac{rate_{N_2}}{rate_{SO_3}} = \sqrt{\frac{M_{SO_3}}{M_{N_2}}} = \sqrt{\frac{80.06 \frac{g}{mol}}{28.014 \frac{g}{mol}}} = 1.691$$

8) Gas "X" diffuses one-eighth as fast as gas "Z". Gas "Z" has a molecular weight = 3.00 g mol⁻¹. What is the molar mass of gas "X".

Answers:

$$\frac{rate_{X}}{rate_{Z}} = \frac{1}{8} = \sqrt{\frac{M_{Z}}{M_{X}}} = \sqrt{\frac{3.00 \text{ g}}{M_{X} \text{ (mol)}}} \text{ Therefore.}$$

$$\left(\frac{1}{8} = \sqrt{\frac{3.00 \text{ g}}{M_{X} \text{ (mol)}}}\right)^{2} = \frac{1}{64} \underbrace{\frac{3.00 \text{ g}}{M_{X} \text{ (mol)}}}_{M_{X} \text{ (mol)}}$$

$$M_{X} = \frac{(64)(3.00 \text{ g})}{\text{(mol)}} = 192 \text{ g mol}^{-1}$$

9) Calculate the average kinetic energy of the molecules in a sample of radon gas at 220 K.

Answers

$$(KE)_{AVE} = \frac{3}{2} \left(\frac{8.31 \ J}{mol \ K} \right) (220 \ K) = 2.7 \times 10^3 \ J \ mol^{-1}$$